What is claimed is:

1. A polyvinyl alcohol obtained by hydrolysis of a polyvinyl ester comprising polymerized silyl group functionalized monomer units of formula (1):

$$(R^{1})_{m}$$
  
| -Si- $(R^{2})_{3-m}$  (1)

wherein R<sup>1</sup> represents an alkyl group having from 1 to 5 carbon atoms; R<sup>2</sup> represents an alkoxyl or acyloxyl group; and m is an integer of from 0 to 2,

which satisfies the following formulae (I):

$$20 < Pw \times S < 460$$
 (I)

wherein Pw is the weight average degree of polymerization of the polyvinyl alcohol; and S is the content (mol%) of the silyl group functionalized monomer units of formula (1) in the polyvinyl alcohol, and

wherein the weight fraction of the polyvinyl alcohol molecules having a degree of polymerization that is more than 3 times the weight-average degree of polymerization of the entire amount of polyvinyl alcohol is at most 25% by weight of the polyvinyl alcohol.

- 2. The polyvinyl alcohol as claimed in claim 1, wherein the weight fraction of the polymer molecules having a degree of polymerization that is smaller than 1/2 times the weight average degree of polymerization of the entire amount of polyvinyl alcohol is at most 12% by weight.
- 3. The polyvinyl alcohol as claimed in claim 1, which satisfies the following formula (II):

$$0.1/100 \le (A - B)/(B) \le 50/100$$
 (II)

wherein A is the silicon atom content of the polyvinyl alcohol in ppm; B is the silicon atom content of the polyvinyl alcohol in ppm after the polyvinyl alcohol has been washed with a sodium hydroxide-containing methanol solution and then washed by Soxhlet extraction with methanol, and A and B are measured by ICP emission spectrometry of an ashed sample of the polyvinyl alcohol, and

wherein an aqueous 4 % solution of the polyvinyl alcohol has a pH of from 4 to 8.

4. A coating agent that contains the polyvinyl alcohol of any one of claims 1 to 3.

- 5. A coated article produced by applying the coating agent of claim 4 to a substrate.
- 6. An inkjet recording material produced by applying the coating agent of claim 4 to a substrate.
- 7. A thermal recording material produced by applying the coating agent of claim 4 to a substrate.
- 8. The polyvinyl alcohol as claimed in claim 1, wherein R<sup>2</sup> is an alkoxyl or acyloxyl group having an oxygen-containing substituent.
  - 9. The polyvinyl alcohol as claimed in claim 1, wherein  $50 < Pw \times S < 420$ .
  - 10. The polyvinyl alcohol as claimed in claim 1, wherein  $100 < Pw \times S < 390$ .
  - 11. The polyvinyl alcohol as claimed in claim 3, wherein  $0.3/100 \le (A-B)/(B) \le 25/100$ .
  - 12. The polyvinyl alcohol as claimed in claim 3, wherein  $0.4/100 \le (A-B)/(B) \le 20/100$ .
- 13. The polyvinyl alcohol as claimed in claim 1 having a degree of hydrolysis of at least 98 mol%.
- 14. The polyvinyl alcohol as claimed in claim 1, wherein the hydrolyzed silyl group functionalized monomer units are present in an amount of from 0.05 to 1.0 mol%.
- 15. The polyvinyl alcohol as claimed in claim 1, wherein the hydrolyzed silyl group functionalized monomer units are present in an amount of from 0.2 to 0.5 mol%.
  - 16. A method for producing the polyvinyl alcohol of claim 1, which comprises:

copolymerizing a vinyl ester monomer with a monomer having a silyl group of formula (1) to form a polyvinyl ester:

$$(R^{1})_{m}$$
  
 $|$  (1)  
 $-Si-(R^{2})_{3-m}$ 

wherein R<sup>1</sup> represents an alkyl group having from 1 to 5 carbon atoms; R<sup>2</sup> represents an alkoxyl or acyloxyl group; and m is an integer of from 0 to 2,

and then hydrolyzing the polyvinyl ester.

17. The method as claimed in claim 16, wherein the monomer is represented by formula (2):

$$(R^{1})_{m}$$
 (2)  
 $CH_{2}=CH-(CH_{2})_{n}-Si-(R^{2})_{3-m}$ 

wherein R<sup>1</sup> represents an alkyl group having from 1 to 5 carbon atoms; R<sup>2</sup> represents an alkoxyl or acyloxyl group; m indicates an integer of from 0 to 2; and n is an integer of from 0 to 4,

or by formula (3):

$$CH_2 = CR^3 - CN - R^5 - Si - (R^2)_{3-m}$$
(3)

wherein R<sup>1</sup> represents an alkyl group having from 1 to 5 carbon atoms; R<sup>2</sup> represents an alkoxyl or acyloxyl group; R<sup>3</sup> represents a hydrogen atom or a methyl group; R<sup>4</sup> represents a hydrogen atom, or an alkyl group having from 1 to 5 carbon atoms; R<sup>5</sup> represents an alkylene group having from 1 to 5 carbon atoms, or a divalent hydrocarbon group that contains an oxygen or nitrogen atom; and m is an integer of from 0 to 2.

- 18. The method as claimed in claim 16, wherein R<sup>2</sup> is an alkoxyl or acyloxyl group having an oxygen-containing substituent.
- 19. The method as claimed in claim 16, wherein the vinyl ester monomer is vinyl acetate and the monomer having a silyl group of formula (1) is vinyl trimethoxy silane.